



## TREE RELATIVELY PRIME CORDIAL GRAPH

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### Abstract

Let  $G = (V, E)$  be a graph with  $p$  vertices and  $q$  edges. A Analytic Mean Cordial Labeling of a Graph  $G$  with vertex set is a bijection from  $v = \{1, 2, \dots, p\}$ . The induced edge labelling are defined by  $f(u, v) = 0$  if either  $f(u)$  divides  $f(v)$  (or)  $f(v)$  divides  $f(u)$  one otherwise and if any one of the vertex label is 1, the induced edge label is 0.

The graph that admits a Relatively Prime Cordial Graph is called Relatively Prime Cordial Graph. In this paper, we proved that path related graphs  $(K_{1,n}; n)$ ,  $K_{1,n}$ ,  $B_{n,n}$ ,  $Hd_n$  Relatively Prime Cordial Graph.

### Introduction

A graph  $G$  is a finite non-empty set of objects called vertices together with a set of unordered pairs of distinct vertices of  $G$  which is called edges. Each pair  $e = \{u, v\}$  of vertices in  $E$  is called an edge or a line of  $G$  in which  $e$  is said to join  $u$  and  $v$ . We write  $e = uv$  and say that  $u$  and  $v$  are adjacent vertices (sometimes denoted as  $u$  adj  $v$ ); vertex  $u$  and the edge  $e$  are incident with each other, as are  $v$  and  $e$ . If two distinct edges  $e_1$  and  $e_2$  are incident with a common vertex, then they are called *adjacent edges*. A graph with  $p$  vertices and  $q$  edges is called  $(p, q)$  – graph. In this paper, we proved that path related graphs  $(K_{1,n}; n)$ ,  $K_{1,n}$ ,  $B_{n,n}$ ,  $Hd_n$  are Relatively Prime Cordial Graph. For graph theory terminology, we follow [2].

### Preliminaries

Let  $G = (V, E)$  be a graph with  $p$  vertices and  $q$  edges. A Analytic Mean Cordial Labeling of a Graph  $G$  with vertex set is a bijection from  $v = \{1, 2, \dots, p\}$ . The induced edge labelling are defined by  $f(u, v) = 0$  if either  $f(u)$  divides  $f(v)$  (or)  $f(v)$  divides  $f(u)$  one otherwise and if any one of the vertex label is 1, the induced edge label is 0.

The graph that admits a Relatively Prime Cordial Graph is called Relatively Prime Cordial Graph. In this paper, we proved that path related graphs  $(K_{1,n}; n)$ ,  $K_{1,n}$ ,  $B_{n,n}$ ,  $Hd_n$  are Relatively Prime Cordial Graph.

#### Definition: 2.1

**Subdivided star** is a graph obtained as oone point union of  $n$  paths of path length 2. It is denoted by  $(K_{1,n}; n)$

#### Definition: 2.2

Star of length one is joined with every vertex of a path  $P_n$  through an edge. It is denoted by  $K_{1,n}$ .

#### Definition: 2.3

In Bistar the root of a star  $S_m$  and  $S_n$  is joined through a vertex  $w$ . It is denoted by  $\langle B_{m,n,w} \rangle$

#### Definition: 2.4

$H$  is a graph obtained from a path  $P_n$  by attaching a pendent edge to every internal vertices of the path. It is called Hurdle graph with  $n-2$  hurdles and is denoted by  $Hd_n$

### Main results

#### Theorem 3.1

Sub divided star  $\langle K_{1,n}; n \rangle$  is Relatively Prime Cordial Graph

#### Proof

Let  $G$  be  $\langle K_{1,n}; n \rangle$

Let  $V(G) = \{u, u_i, v_i, w_i, z_i; 1 \leq i \leq \frac{n}{2}\}$

Let  $E(G) = \{(u u_i); 1 \leq i \leq \frac{n}{2}\} \cup \{(u v_i); 1 \leq i \leq \frac{n}{2}\} \cup \{(u_i w_i); 1 \leq i \leq \frac{n}{2}\} \cup \{(v_i z_i); 1 \leq i \leq \frac{n}{2}\}$

Define  $f : V(G) \rightarrow \{1, 2, \dots, p\}$

Vertex Labeling:

$$f(u) = 2$$



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$$\begin{aligned}
 f(u_i) &= 4i & 1 \leq i \leq \frac{n}{2} \\
 f(v_i) &= 4i - 1 & 1 \leq i \leq \frac{n}{2} \\
 f(w_i) &= 4i + 2 & 1 \leq i \leq \frac{n}{2} \\
 f(z_i) &= 4i + 1 & 1 \leq i \leq \frac{n}{2}
 \end{aligned}$$

Edge Labeling:

$$\begin{aligned}
 f^*(uu_i) &= 0 & 1 \leq i \leq \frac{n}{2} \\
 f^*(uv_i) &= 1 & 1 \leq i \leq \frac{n}{2} \\
 f^*(u_iw_i) &= 0 & 1 \leq i \leq \frac{n}{2} \\
 f^*(v_iz_i) &= 1 & 1 \leq i \leq \frac{n}{2}
 \end{aligned}$$

Here, When  $n=m$

$$\begin{aligned}
 e_f(0) &= 2m \\
 e_f(1) &= 2m
 \end{aligned}$$

$$|e_f(1) - e_f(0)| \leq 1$$

Hence, Sub divided star  $\langle K_{1,n}; n \rangle$  is Relatively Prime Cordial Graph.

For example, The Relatively Prime Cordial Graph of Sub divided star

$\langle K_{1,n}; n \rangle$  are shown in the figure

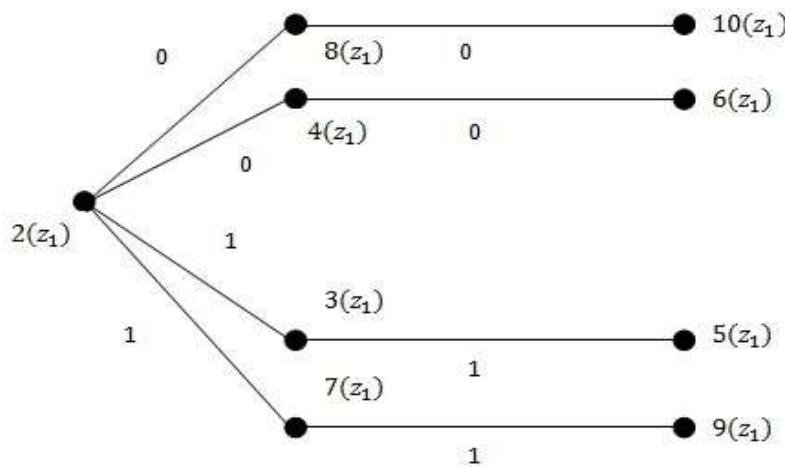


Figure 3.1

**Theorem:3.2**

$K_{1,n}$  is a Relatively Prime Cordial Graph.

**Proof:**

Let G be  $(K_{1,n})$

Let  $V(G) = \{u, u_i: 1 \leq i \leq n\}$

Vertex Labeling:

$$\text{Let } E(G) = \{(uu_i): 1 \leq i \leq n\}$$

$$\begin{aligned}
 f(u) &= 2 \\
 f(u_i) &= i + 2 & 1 \leq i \leq n
 \end{aligned}$$

Edge Labeling:



$$f^*(u_i) = \begin{cases} 1 & i \equiv 1 \pmod{2} \\ 0 & i \equiv 0 \pmod{2} \end{cases} \quad 1 \leq i \leq n$$

Here, When  $n=2m$

$$e_f(0) = m$$

$$e_f(1) = m$$

When  $n = 2m + 1$

$$e_f(0) = m$$

$$e_f(1) = m + 1$$

$$|e_f(1) - e_f(0)| \leq 1$$

Hence,  $K_{1,n}$  is Relatively Prime Cordial Graph.

For example, The Relatively Prime Cordial Graph of Sub divided star  $(K_{1,n})$  are shown in the figure

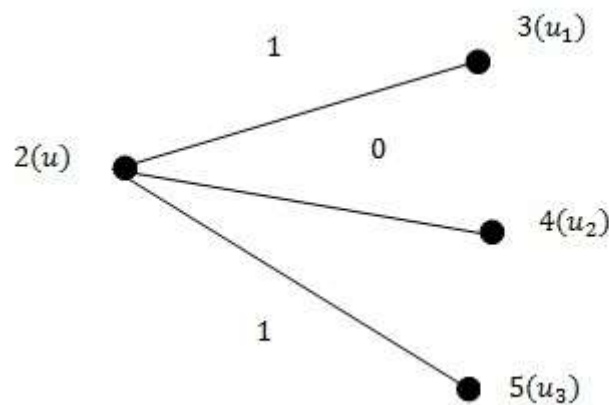


figure 3.2

**Theorem:3.3**

Bistar  $B_{n,n}$  is Relatively Prime Cordial Graph.

**Proof:**

Let  $G$  be  $B_{n,n}$

Let  $V(G) = \{u, v, u_i, v_i; 1 \leq i \leq n\}$

Let  $E(G) = \{(uv)\} \cup \{(u_i u_i); 1 \leq i \leq n\} \cup \{(v_i v_i); 1 \leq i \leq n\}$

Define  $f : V(G) \rightarrow \{1, 2, \dots, p\}$

Vertex Labeling:

$$f(u) = 1$$

$$f(v) = 2$$

$$f(u_i) = 2i + 2 \quad 1 \leq i \leq n$$

$$f(v_i) = 2i + 1 \quad 1 \leq i \leq n$$



Edge Labeling:

$$\begin{aligned}
 f^*(uv) &= 0 \\
 f^*(uu_i) &= 0 \quad 1 \leq i \leq n \\
 f^*(vv_i) &= 1 \quad 1 \leq i \leq n
 \end{aligned}$$

Here, when  $n = m$

$$\begin{aligned}
 e_f(0) &= m + 1 \\
 e_f(1) &= m
 \end{aligned}$$

$$|e_f(1) - e_f(0)| \leq 1$$

Hence,  $B_{n,n}$  is Relatively Prime Cordial Graph.

For example, The Relatively Prime Cordial Graph of Sub divided star  $B_{n,n}$  are own in the figure

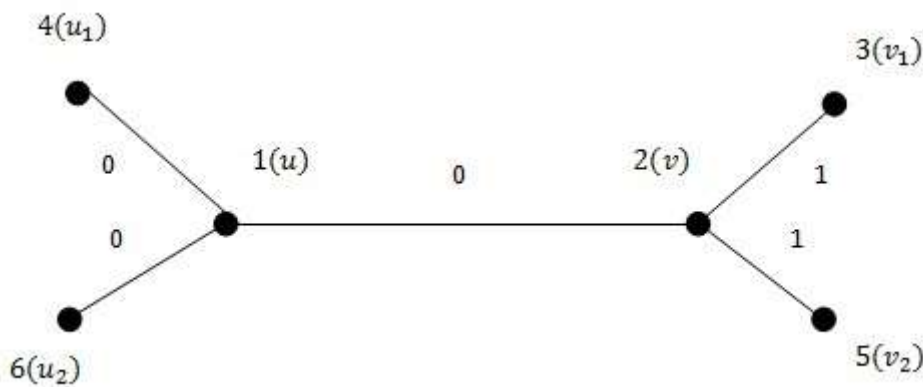


figure 3.3

**Theorem 3.4**

Graph  $Hd_n$  is a Relatively Prime Cordial Graph.

**Proof:**

Let  $G$  be  $Hd_n$

$$V(G) = \{[u_i; 1 \leq i \leq n], [v_i; 1 \leq i \leq n - 2]\}$$

$$E(G) = \{[(u_i u_{i+1}): 1 \leq i \leq n - 1] \cup [(v_i v_{i+1}): 1 \leq i \leq n - 2]\}$$

$$Define f : V(G) \rightarrow \{1, 2, \dots, p\}$$

Vertex Labeling:

$$\begin{aligned}
 f(u_i) &= 2i \quad 1 \leq i \leq n \\
 f(v_i) &= 2i + 1 \quad 1 \leq i \leq n
 \end{aligned}$$

Edge Labeling:

$$\begin{aligned}
 f^*(u_i u_{i+1}) &= 0 \quad 1 \leq i \leq n - 1 \\
 f^*(v_i v_{i+1}) &= 1 \quad 1 \leq i \leq n - 2
 \end{aligned}$$



Here, When  $n = m$

$$e_f(0) = m - 1$$

$$e_f(1) = m - 2$$

$$|e_f(1) - e_f(0)| \leq 1$$

Hence,  $Hd_n$  is Relatively Prime Cordial Graph.

For example, The Relatively Prime Cordial Graph of  $Hd_n$  are shown in the figure

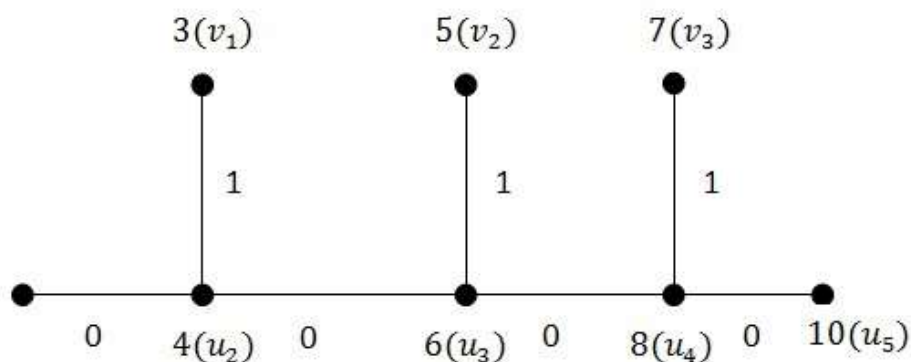


Figure 3.4

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